

AD A 040954

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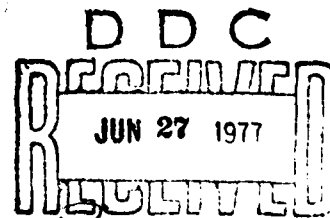
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Prepared for the 14th Annual Meeting of the JANNAF  
Structures and Mechanical Behavior Working Group held  
at the Johns Hopkins University, Applied Physics  
Laboratory, Laurel, Maryland on February 15-17, 1977.

Contract No. N00014-72-C-4481

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## CRACK PROPAGATION IN DOUBLE-BASE PROPELLANTS

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### ABSTRACT

Crack propagation tests were conducted on a composite modified double-base (CMDB) propellant with the use of center-cracked strip biaxial specimens. Constant strain rate tests were conducted at several temperatures (40° to 105° F) and crosshead rates (0.02 to 200 in./min) to define the crack initiation and propagation characteristics for monotonically increasing strain history. The tests were conducted at ambient, 250, and 500 psig pressure to evaluate the effect of pressure on initiation and crack velocity. A second series of tests was conducted to evaluate the effect of a prestrain damage history on crack propagation. In the second series, the samples (without precut cracks) were initially prestrained to 15 to 25 percent and held for a period of time to induce material damage. After load release and sufficient recovery time, cracks were inserted in the specimens and they were then pulled to failure at a constant strain rate. Similar tests were conducted on round, notched tensile samples to define the critical stress intensity factor ( $K_{Ic}$ ) and to provide a comparison between uniaxial and biaxial fracture initiation. Schapery's viscoelastic fracture theory was used to evaluate the crack velocity data under constant strain rate conditions. One important result of the study was the finding that the crack velocity depended rather strongly on imposed strain level.

### INTRODUCTION

Crack initiation and propagation in polymeric materials has been given considerable attention during the last 15 years, stimulated primarily by their unique viscoelastic behavior and also by the use of polymers as solid propellant rocket fuels. Filled polymers are used extensively as solid propellant grains which must undergo a variety of environmental loading conditions, during motor storage and handling and during actual operational firing conditions, which impose pressure loads at high rates and for relatively long times. The consequence of a crack can be the failure of the rocket motor as a result of overpressurization, case burn-through, erratic pressure-time response, or a variety of events related to structural or ballistic performance failure. The primary work over the last decade has been aimed at defining the laws which govern crack initiation, propagation, and trajectory under motor-like operational conditions to arrive at an assessment of overall crack criticality for a given rocket motor system.

A number of investigators have studied viscoelastic crack propagation in polymers and solid propellants (1-10). Most of the early work was done

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along the lines of classical elasticity using the Griffith solution for crack initiation. Bennett (11,12) presented the first known data on solid propellant crack initiation in a state-of-the-art composite propellant and noted that the fracture energy,  $\Gamma$ , was time- and temperature-dependent. Use of the data for motor applications was made on the basis of an energy balance using finite element analysis. Correlation of the data with that from analysis using the thermodynamic power balance and the Williams' spherical flaw model was not quantitatively satisfactory (4,11). No attempt was made to monitor crack velocity during the tests. Only crack initiation was monitored by visual observation.

Knauss (5-8,13) and Schapery (14,15) have made significant contributions to theoretical portion of the problem of viscoelastic crack propagation. Knauss (5,8) developed an approximate solution for a line crack problem which incorporates a failure zone length to introduce time and velocity effects. Knauss and Mueller (5,6) applied the theory to an unfilled polyurethane polymer with encouraging results achieved for a variety of loading environments.

Using a stress intensity approach to fracture of solid propellant grains, Francis et al (16,17) conducted a program on an unfilled polyurethane polymer (Solithane 113), an epoxy, and later, a PBAN composite propellant formulation. The primary contributions of their work was the discovery that superimposed pressure causes about a 30 to 40 percent increase in the stress intensity factor at a given crack velocity, thus requiring more energy to propagate the crack. This fact was essentially known, or assumed from superimposed pressure tensile tests, but was not directly related to actual crack propagation experimental data per se. The thermal and pressure loading data on small, two-dimensional samples of Solithane 113, obtained by a stress intensity factor approach, were encouraging.

Swanson (18) was the first to apply fracture mechanics to composite modified double-base (CMDB) propellant. He performed a stress analysis of small, precracked, subscale STV motors formulated in terms of stress intensity factors. Using quasi-elastic analysis and time-dependent critical stress intensity factors, he was reasonably successful in predicting crack initiation in the STV subscale motors subjected to high-rate pressurization tests.

The problem of crack propagation in solid propellants has only been briefly mentioned in previous literature, leaving vast areas untouched. This is particularly true for the solid rocket motor grain itself, which must undergo a wide range of environments and loading conditions not heretofore studied in the laboratory either experimentally or analytically. Schapery (15,16) has recently been working on a more generalized approach which may be able to resolve more complicated load histories representative of actual motor conditions. Schapery generalized the Barenblatt model (19) for elastic fracture to linear viscoelastic conditions and then developed the governing equations for crack velocity in terms of the linear viscoelastic material properties.

Swanson (20) recently used the Schapery theory to evaluate published data on a PBAN composite propellant and found that there was a very good agreement between theory and experiment over a large range of variables. Swanson found a time-dependent fracture energy,  $\Gamma$ , for both crack initiation and crack propagation must be assumed whereas  $\Gamma$  constant could be assumed for Solithane 113.

The present program was aimed at evaluating the Schapery theory when it was applied to a CMDB propellant under similar loading conditions. CMDB propellant generally is different than composite propellant as it has a granular filler material of a characteristic length of 0.05 to 0.07 inch and uses a nitrocellulose binder matrix instead of polyurethane and polybutadiene. Aside from the more standard loading environments of temperature, pressure, and rate (time), it was also of interest to compare multiaxial effects (uniaxial versus biaxial) and investigate the effects of prestraining damage on crack propagation characteristics. The latter is of interest to predict the behavior of a crack in a motor which must undergo previous loading history before actual ignition loads, a situation which is the case for most all missile systems in use today.

#### THEORETICAL BACKGROUND

##### Schapery's Theory of Viscoelastic Fracture

Schapery's theory of viscoelastic fracture, as well as some application to available polymeric materials, is discussed in References 15 and 16. For completeness, the main highlights are reviewed in this paragraph, since the CMDB propellant data will be considered with respect to the existing theory in later paragraphs.

Schapery develops the theory for the time-dependent size and shape of cracks in linearly viscoelastic, isotropic media for Mode I (tensile) opening stress conditions. The proposed model assumes that failure occurs in a small region behind the crack tip and is essentially equivalent to the Barenblatt model (19), except that no restriction is made on the constitutive properties of the material in the failure zone. Linear viscoelastic theory predicts the boundary around the crack tip to be cusp-shaped, a geometry which is based on the assumption of linear viscoelastic behavior in the surrounding material and which is demonstrated in several solid propellants. The singularity in stress at the crack tip due to the cohesive forces in the failure zone is equated to the negative of the singularity in stress at the crack tip due to the external applied load, so that the resulting stress is everywhere finite. Schapery calculates the work done on the cohesive (failure) zone by the surrounding linear viscoelastic material and equates this to the fracture energy,  $\Gamma$ . The relationship for the crack velocity is then developed in the form

$$\Gamma = \frac{C_v (\bar{t}_a) K_I^2}{8} \quad (1)$$

where:

$\Gamma$  = Fracture energy required to produce one unit of new surface area

$C_v$  = Related to creep compliance of surrounding material

$\tilde{t}_\alpha$  = Characteristic time

$K_1$  = Opening mode stress intensity factor

The characteristic time,  $\tilde{t}_\alpha$ , is related to the length of the failure zone,  $\alpha$ , and the crack velocity,  $\dot{a}$ , by

$$\tilde{t}_\alpha = \frac{\alpha}{3\dot{a}} \quad (2)$$

where the time may be viewed as that required for the crack to traverse the failure zone at the crack tip.  $C_v$  is proportional to the uniaxial plane strain creep compliance which, for a constant value of Poisson's ratio, is given by

$$C_v(t) \approx 4(1 - \nu^2)D(t) \quad (3)$$

Compliance (and modulus) data for polymeric materials may often be expressed as a power law in time. For a one- or two-term power law representation of  $C_v$ , equation (1) can be solved explicitly for the crack velocity as

$$\dot{a} = \left[ \frac{C_1 \lambda_n \pi^n}{\Gamma \sigma_m^{2n} I_1^{2n} 2^{3+n}} \right]^{1/n} K_1^{2(1+1/n)} \quad (4)$$

where:

$$C_v \equiv C_1 t^n$$

$\sigma_m, I_1 \equiv$  Constants or material parameters defined by Schapery for the failure zone

If one can assume that the fracture energy,  $\Gamma$ , is a constant, then the propagation law, equation (4), may be written in the form

$$\dot{a} = A K_1^{2(1+1/n)} = A K_1^q \quad (5)$$

where  $A$  becomes the term in the brackets  $\left[ \right]$  in equation (4) for constant values of  $\Gamma$  and  $\sigma_m I_1$ .

Swanson (20) discusses some of the possibilities of equation (5) if  $\Gamma$  is not constant and evaluates PBAN propellant data for a time-dependent value of  $\Gamma$ . However, the key result of Schapery's analysis is that crack propagation fracture energy cannot depend on higher order derivatives of crack motion or histories of crack motion. For purposes of this paper, the functional dependence of  $\Gamma$  was not investigated but

restricted to the general behavior already noted in the original objectives. Equation (5) says that the relationship between the stress intensity factor ( $K_1$ ) and crack velocity ( $\dot{a}$ ) is linear when plotted on log-log paper and has a slope proportional to the exponential ( $q$ ).

#### Extension of Theory to Constant Strain Rate Tests

Since the data to be presented in subsequent sections were derived from constant strain rate tests, the crack growth law will be reformulated for the particular test at hand.

In the constant strain rate test, the applied stress,  $\sigma$ , is derived from the Boltzmann superposition integral for isothermal conditions as

$$\sigma(t) = R_{\epsilon} \int_0^t E_{\text{Rel}}(t - r) dr \quad (6)$$

which, for the power law relaxation modulus given by

$$E_{\text{Rel}}(t) \equiv E_1 t^{-n} \quad (7)$$

results in

$$\sigma(t) = \frac{R_{\epsilon} E_1 t^{1-n}}{(1 - n)} \quad (8)$$

where:

$R_{\epsilon}$  = Strain rate

$E_1, n$  = Power law material constants

It should be noted that the applied stress ( $\sigma$ ) is the far field stress which would be present for an infinite strip. The necessary correction factors for finite strip width will be discussed in the following paragraphs.

For a centrally cracked plate of infinite width, the stress is related to the stress intensity factor,  $K_1$ , and the half-crack length,  $a$ , by the expression

$$K_1 = \sigma \sqrt{\pi a} \quad (9)$$

The crack growth may be expressed in terms of the applied stress ( $\sigma$ ) by integrating equation (4), using the chain rule to change the independent variable from time to stress, and using the relationship between time and

stress, equation (8), to get

$$\frac{a}{a_0} = \left[ 1 - C_4 (a_0)^{1/r} (\sigma^P - \sigma_c^P) \right]^{-r} \quad (10)$$

where equation (9) has been used to express the stress intensity factor in terms of applied stress, and where

$$C_4 = \frac{A}{r} \left( \frac{\pi^{q/2}}{1-n} \right) \left( \frac{1-n}{R_\epsilon E_1} \right)^{\frac{1}{1-n}} \frac{1}{P} \quad (11a)$$

$$P = q + \frac{1}{1-n} \quad (11b)$$

$$q = \text{experimental value from Equation (5)} \quad (11c)$$

$$r = \frac{2}{q-2} \quad (11d)$$

$$\sigma_c = \text{critical stress} \quad (11e)$$

Equation (11) holds when the fracture energy  $\Gamma$  is a constant, the assumption used to evaluate the CMDB data.

#### Finite Geometry Correction Factors

The determination of stress intensity factors from experimental data generated by finite width centrally-cracked strip biaxial specimens requires geometry correction factors. Isida (21) generated correction factors for finite width and height for the strip biaxial sample subjected to several types of loading boundary conditions. The factors given in (21) were verified and extended over a wider range of variables by using the TEXTGAP (22) finite element program. The values of  $K_I$  determined over the range of interest showed very good agreement with the original Isida values. TEXTGAP and Isida values were usually within 1 to 2 percent of each other. A subroutine was written for eventual data reduction and consisted of the correction factors for finite width and height, allowing for crack growth and boundary displacement.

#### EXPERIMENTAL PROGRAM

Crack initiation and propagation tests were conducted in a series of experiments which involved both uniaxial and biaxial tensile tests. The uniaxial tests were used to generate fracture toughness ( $K_{Ic}$ ) for uniaxial stress field conditions. The biaxial tests were designed to provide fracture toughness ( $K_{Ic}$ ) values as a comparison, but, moreover, the tests were primarily used to furnish crack velocity data as a function of the imposed stress intensity factor ( $K_I$ ) for a variety of environmental conditions.

The propellant used in the program is a CMBB formulation designated EJC. The propellant was taken from an 8-year old Polaris second stage motor. Typical uniaxial tensile properties are 195 psi maximum stress, 50 percent strain at maximum stress, and 570 psi initial modulus. The experimental program which was carried out is discussed in the following paragraphs.

#### Uniaxial Fracture Toughness ( $K_{Ic}$ )

The sample used to generate uniaxial fracture toughness ( $K_{Ic}$ ) values is shown in Figure 1. The sample is rough-cut by saw from bulk propellant removed from a sectioned motor and subsequently machined on a lathe into the desired configuration. The crack, in the form of a circumferential notch, is inserted to a known depth with an X-acto knife mounted on the lathe fixture during the machining operation. Because of the nature of the test and specimen configuration, there is not believed to be any significant difference in  $K_{Ic}$  as a result of the artificial crack in comparison with a natural crack. Crack growth in this specimen is relatively fast and should not indicate any difference in behavior as a result. Once the samples are machined they are end-bonded to metal tab cylinders prior to testing.

The samples were pulled at crosshead rates ranging from 0.02 to 200 inches per minute with an Instron test machine for the lower rates and a closed-loop hydraulic machine for the higher rates. The effect of temperature was determined over a range from 20° to 105° F. Since pressure is often a strong influence on the fracture characteristics of composite rubber-base propellants, the tests were also conducted at superimposed pressures of 0, 250, 500, and 1000 psig with a pressure chamber around the sample. Care was taken to ensure that the sample was not damaged due to handling and pretest loads during grip insertion.

#### Biaxial Fracture Characteristics

The crack initiation and propagation behavior in a biaxial stress field was defined through the use of centrally cracked strip biaxial specimens as shown in Figure 2. As with the uniaxial samples, the strip biaxial specimens were prepared from bulk propellant by a similar procedure. The specimens were machined to the final configuration, after which the end tabs were bonded on. The end tabs provide the sample loading transition as well as the biaxial stress field due to the lateral bonding constraint. The end tabs were mounted in a special grip which prevents sample rotation during the test, a problem of considerable significance in crack propagation testing.

In this particular study, the crack length ( $2a_0$ ) was selected as 1.5 inches. This length corresponds to the width of commercial, single-edge razor blades, which were used to induce the artificial cracks in the specimens. The cracks were made in the specimens before testing after careful alignment of the cutting blade over the center of the specimen, equidistant from the edges. A transparent, plastic grid is superimposed over the crack area and taped in place near the grips to provide a reference base during the crack growth period. The crack

pattern was made more distinct by placing a sheet of white paper on the back side of the tan-colored specimen to assist in the final photo analysis. Crack initiation and propagation were recorded and assessed through the use of slow motion (low rate tests) and high speed (moderate-to-high rate tests) photography at frame rates up to 5000 frames per second.

The primary tests were conducted at crosshead rates ranging from 0.02 to 200 inches per minute with the Instron and closed-loop hydraulic test machines. The tests were run at temperatures of 40°, 77°, and 105° F after an equivalent dummy sample (same thickness) indicated temperature equilibration. The effect of superimposed pressure was also investigated at 77° F for pressure levels of 250 and 500 psig. The crack growth characteristics for the thermal tests were observed by mounting a plexiglass door on the temperature chamber, while those for the pressure tests were observed through a 4-inch thick plexiglass window on the pressure chamber. Optical clarity in the pressure tests was particularly good, since the sample was located relatively close to the window and external lighting could be readily used. Care was taken to ensure that sample surface heating was avoided by using the lights only during the camera recording bursts and by keeping the burst periods short (10 seconds or less). The reference time was determined by the camera system (electronic frequency counter) or by a stopwatch located in the viewing area.

A second series of tests was conducted to evaluate the effects of pre-strain material damage on crack propagation behavior. In this series, the strip biaxial samples selected for the study were pulled to predetermined strain levels of 15 and 25 percent at the crosshead rate of 2 inches per minute and then held for 30 minutes. The samples were then unloaded and allowed to relax overnight before retesting. The cracks were inserted after the recovery period and just before the retesting. The tests were conducted at ambient pressure at temperatures of 40°, 77°, and 105° F and crosshead rates of 0.02, 2, and 200 inches per minute by the same procedures used for the virgin samples.

Stress relaxation modulus data, necessary for evaluation of crack growth behavior, was available from Reference 23. These data were obtained on round, end-bonded samples similar to the notched fracture toughness sample shown in Figure 1. The strain level used for these data was typically 1/2 to 1 percent strain. The data are shown fitted to the power law form

$$E(t) = E_1 t^{-n} \quad (\text{See Eq 7})$$

where  $E_1$  and  $n$  are material constants for the particular CMDB propellant. The power law fit works well over the seven decades of time shown in Figure 3.

#### DISCUSSION OF RESULTS

##### Uniaxial and Biaxial Fracture Toughness ( $K_{Ic}$ )

The critical stress intensity factor, or fracture toughness ( $K_{Ic}$ ), determined from the uniaxial round notched and strip biaxial sample is

shown in Figure 4 as a function of the time-to-failure,  $t_f$ . Several comments should be made concerning the method of data reduction. The value of  $K_{Ic}$  for the notched, round tensile specimen was derived from a solution by Bueckner (24) and given by

$$K_{Ic} = \sigma_{mn} \sqrt{\pi D} F(d/D) \quad (12)$$

where:

$D$  = Outside diameter

$d$  = notched section diameter

$\sigma_{mn}$  = Net section stress determined at maximum load

$F(d/D)$  = Geometrical correction factor shown in (24)

The photo analysis of the strip biaxial samples was used to provide the value of  $K_{Ic}$  from the time at which the crack was visually observed to crack. The computer subroutine automatically input the correction factors for finite width and height. In summary, the uniaxial  $K_{Ic}$  was determined from the maximum load whereas the biaxial  $K_{Ic}$  was determined from visual observation of crack growth.

There does not appear to be any difference in behavior between uniaxial and biaxial crack initiation in the CMDB propellant. The two methods of  $K_{Ic}$  determination should not be significantly different, since the notched round tensile sample would be expected to exhibit rather fast crack growth from initiation to sample separation. Pressure also does not significantly affect the time-to-failure for the CMDB propellant. The functional form of Figure 4 fits

$$t_f = B K_{Ic}^{-7.11} \quad (13)$$

where:

$$B = 9.2 (10^{-16})$$

#### Effect of Strain Rate

The evaluation of the load-time traces and the film records by using the correction factors for finite width and height results in the experimental relationship between stress intensity factors and crack velocity as shown in Figure 5. The solid lines represent the data from four replicate tests at any one given rate and typically show less than 10 percent variation. Any individual curve, for a given rate, follows the form derived by Schapery in equation (5) with the values given by

$$\dot{a} = A_\epsilon K_I^{2.0} \quad (14)$$

where  $A_2$  depend on the particular strain rate employed. This is unusual since all previously reported data on composite propellants indicate the value of the exponent to be on the order of 6 to 7 and a continuous, smooth curve rather than a dependence on strain rate as shown. However, if one cross plots several values of  $K_1$  and  $\dot{a}$  for a fixed strain level, then it becomes readily apparent that a continuous function is found, but that the crack propagation exhibits a strong nonlinear dependence on strain level. The crack propagation law now takes on the form

$$\dot{a} = A' \epsilon_o K_1^{7.50} \quad (15)$$

where the value of  $A' \epsilon_o$  depends on strain level. The exponent agrees reasonably well with experimental data on composite propellants as well as the value given in equation (13) from the crack initiation data ( $K_{1c}$ ).

There are two important aspects of Figure 5. The first is that the data obey Schapery's power law crack propagation law, equation (5), over several decades of crack velocity. The second and more important aspect is that there is a strong effect of strain level on the crack propagation. This result has not been reported in the literature but is expected to be rather significant in analyzing actual rocket motor situations. Schapery (25) has indicated that this result is not totally unexpected on the basis of nonlinear viscoelastic behavior exhibited in composite propellants.

Closer examination of equations (4) and (5) would indicate that the strain dependence could very easily enter in through the creep compliance or the description of the failure zone. Further work is needed in this area to define this dependence.

#### Temperature and Pressure Effects

The effects of temperature and superimposed pressure on crack propagation are shown in Figures 6 through 8. The effect of temperature follows the familiar time-temperature shifting principles shown in Figure 7. The data were shifted experimentally by using a single rate and temporarily ignoring the strain effect noted earlier. The correct procedure would entail a definition of the crack propagation law for a given strain level, say 10 percent, followed by the shifting procedure. Pressure shows the same effect as lowering the temperature, namely, increasing the stress intensity factor at a given crack velocity. The same effects are seen in composite propellants (16). A pressure enhancement of about 25 to 30 percent on the stress intensity factor is realized with the addition of 500 psig.

#### Prestrain Damage Effects

The tests on strip biaxial samples subjected to various levels of prestrain were conducted primarily to assess the difference in crack propagation as a result of prior load history, namely, a constant strain history to some level  $\epsilon_o$ . Figure 9 shows the result of the tests. At the highest strain rate, 200 in./min crosshead rate, no difference is

seen in the crack propagation behavior after the prestrain damage cycle. Even for prestrain levels as high as 25 percent, no significant difference was exhibited in the response. However, as one goes to lower strain rates, possibly 0.02 in./min crosshead rate, the effect of the prestrain cycle begins to affect the crack propagation response. The effect of the prestrain is to decrease the stress intensity factor at which the crack will propagate for a fixed velocity. Referring to Figure 5, where the effect of strain level on crack propagation was first noted, it can be seen that, at the high strain rates, the propagation takes place at a higher strain level (e.g., 14 to 22 percent). Conversely, at the lower strain rates, the crack propagation begins at much lower strain levels (e.g., <8 percent). Therefore, it would not be expected to see much difference in behavior at the high strain rates for prestrain levels on the order of 15 to 25 percent. The lower strain rates should exhibit a different behavior due to the amount of microcracking which resulted from the 15 to 25 percent prestrain cycle.

#### Comparison with Schapery's Theory

The constant strain rate data shown in Figure 5 was evaluated by using Schapery's theory (15,16) to predict the crack growth from measured material properties and experimental stress values after correcting for finite geometry effects. Using equation (10), after reformulating to the more convenient form

$$\Delta a = a - a_0 \quad (16)$$

the data were used to predict the expected crack growth,  $\Delta a$ . It should be remembered that there is some latitude in empirical fitting of the data in view of the assumptions which can be made regarding  $F$ . However, in viewing the data and theory as shown in Figures 10 through 14, the qualitative fit of the data to the theory appears to be reasonably good, although further work is necessary in light of the strain effect.

#### CONCLUSIONS

The crack propagation behavior of CMDB propellants appear to be qualitatively similar to that previously reported for unfilled polymers (Solithane 113) and PBAN composite propellants. Both propellant systems exhibit strong temperature- and pressure-dependence on crack growth. For the CMDB propellant studied, the uniaxial and biaxial fracture toughness ( $K_{Ic}$ ) are in good agreement, indicating little, if any, difference in multiaxial behavior for crack initiation for opening mode tensile conditions. Comparisons with Schapery's theory shows that the CMDB propellant obeys the power law crack propagation law, equation (5), and agrees qualitatively for the stress-crack growth predictions shown in Figures 10 through 14.

Perhaps the most important results discussed in this paper are the strong effect of strain on crack propagation and the effect of prestrain damage cycles on low strain rate crack propagation behavior. Both of these effects are extremely important if one is to adequately characterize the

material and make reliable grain predictions under thermal or pressure loading conditions.

#### ACKNOWLEDGMENTS

The assistance of Mr. T. D. Pavelka in writing the computer programs for the crack propagation data analysis and of Mr. C. D. Wahlin for performing the data analysis and photographic assessment of the strip biaxial test is greatly appreciated.

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ALL DIMENSIONS IN INCHES

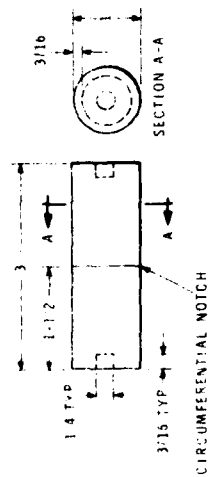


Figure 1. Round-Notched Tensile Sample

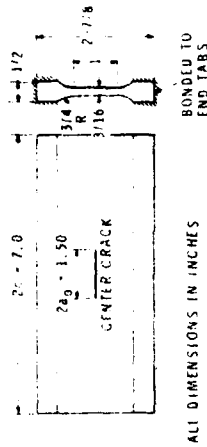


Figure 2. Strip Biaxial Sample

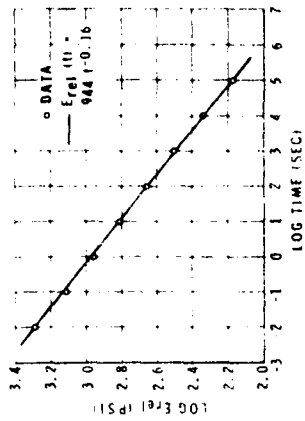


Figure 3. Stress Relaxation Modulus for CMD8 Propellant

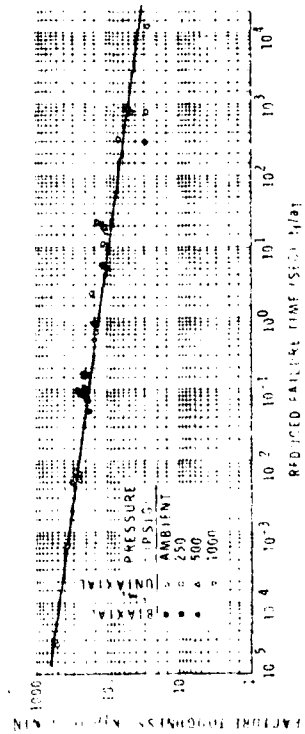


Figure 4. Creep Rate vs. Time for CMD8 Propellant

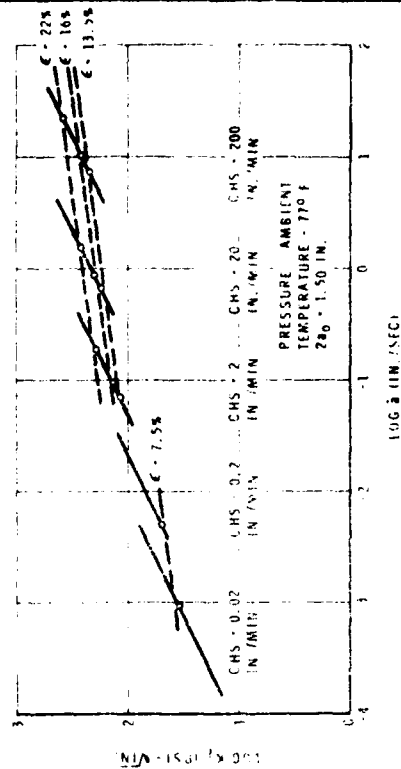


Figure 5. Effect of Strain Rate on Crack Propagation in CMD8 Propellant

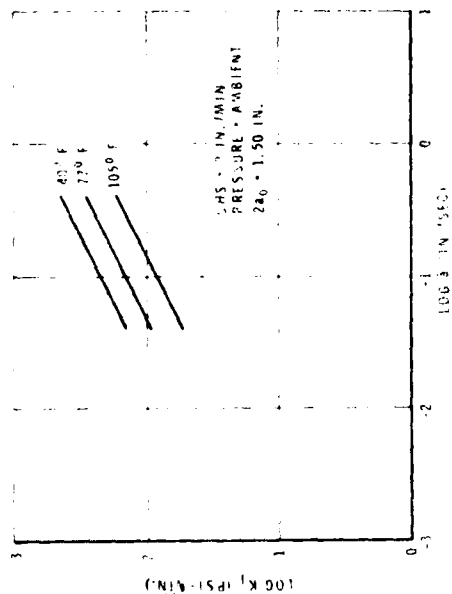


Figure 5. Effect of Temperature on Crack Propagation in CMOB Propellant

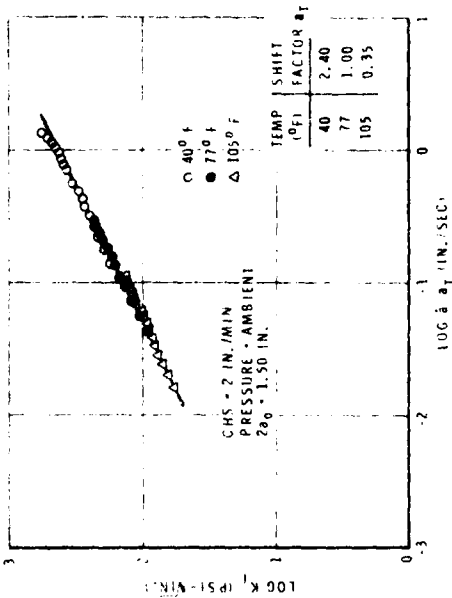


Figure 7. Crack Velocity Versus Stress Intensity Factor Master Curve for CMOB Propellant

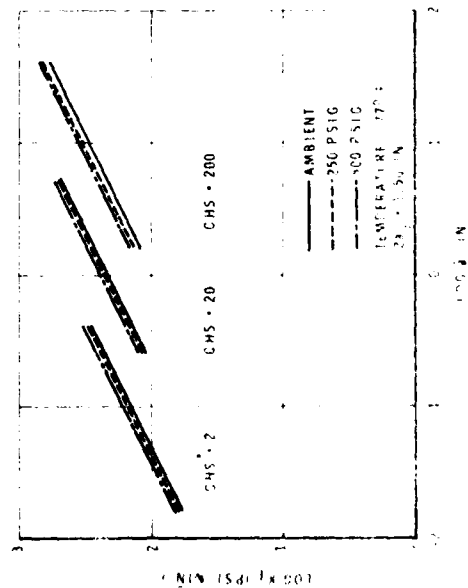


Figure 6. Effect of Pressure on Crack Propagation in CMOB Propellant

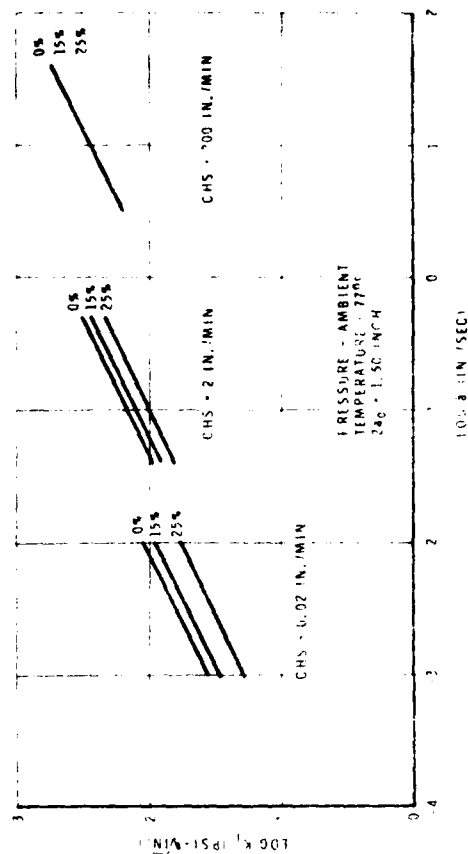


Figure 8. Effect of Pressure on Crack Propagation in CMOB Propellant

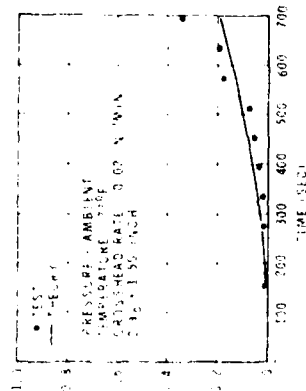


Figure 10. Crack Growth Predictions for 0.02 in./min Crosshead Rate

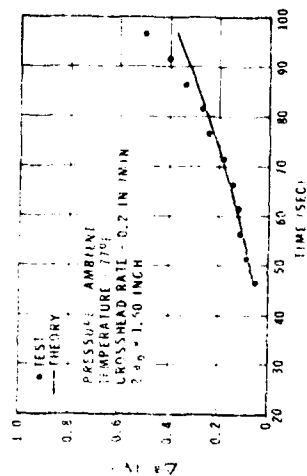


Figure 11. Crack Growth Predictions for 0.2 in./min Crosshead Rate

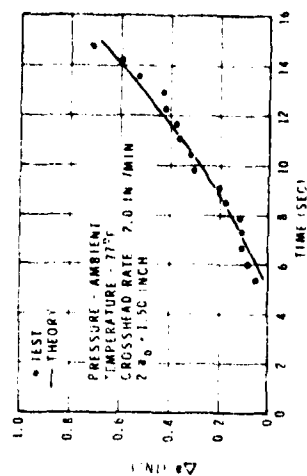


Figure 12. Crack Growth Predictions for 2.0 in./min Crosshead Rate

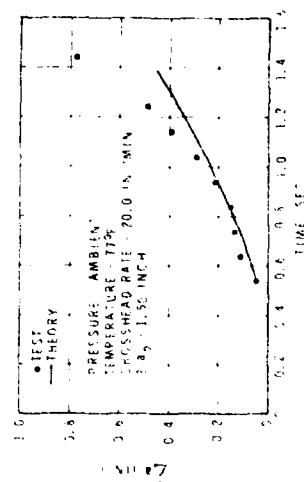


Figure 13. Crack Growth Predictions for 20 in./min Crosshead Rate

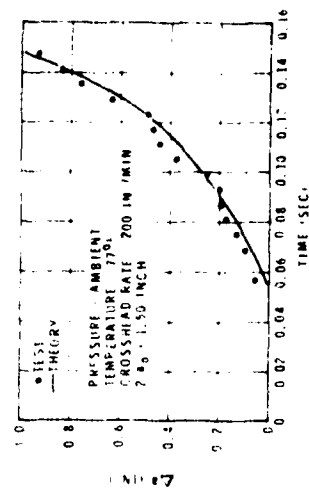


Figure 14. Crack Growth Predictions for 200 in./min Crosshead Rate